# YOUR TITLE GOES HERE

Your name

Advisor: Professor xxx

A Thesis

Presented to the Faculty of the Computer Science Department of Middlebury College

May 2023

# ABSTRACT

Your abstract goes here.

## ACKNOWLEDGEMENTS

Your acknowledgements go here.

# TABLE OF CONTENTS

1	Introduction	1
2	Background2.1Notation2.2Probability	<b>2</b> 2 2
3	Your Work Part 1	3
4	Your Work Part 2	5
5	Conclusion         5.1       Open Problems	<b>6</b> 6
A	Details of Code, Proofs, etc.	7
B	Notes on Writing	9
	B.1 Expectations	9
	B.2 Plagiarism	10
	B.3 Best Practices	10
	B.4 Writing FAQ	11

# LIST OF TABLES

# LIST OF FIGURES

3.1 A non-planar graph.		3
-------------------------	--	---

## INTRODUCTION

### Motivation

Explain why what you are investigating is important.

#### **Previous work**

Explain how what you did relates to previous work. You should reference and describe previous work, but avoid going too far down rabbit holes that are unrelated to the present thesis. You can cite using either a plain citation command to produce a number [2] or by using \textcite to discuss a text by name, like Carroll [2].

## Your work

Briefly explain your results

#### BACKGROUND

Describe background information that is necessary for a moderately experienced computer scientist (think your professors) to understand your thesis.

## 2.1 Notation

Explain relevant notation. For example: Let  $[N] = \{1, 2, ..., N\}$ .

## 2.2 Probability

**Theorem 2.0.1** (Hoeffding's Inequality). Consider independent random variables  $X_1, \ldots, X_n$  where for each variable  $X_i$ , we have  $0 \le X_i \le 1$ . Let  $\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$ .

$$Pr\left(\bar{X} - E[\bar{X}] \ge t\right) \le e^{-2nt^2}.$$
(2.1)

Theorem 2.0.1 gives us an example of referring to a labeled object using the  $\Cref$  macro.

### YOUR WORK PART 1

I first analyzed the graph shown in Fig. 3.1. You can see details of this analysis in Appendix A.



Figure 3.1: A non-planar graph.

To study this process, I used the algorithm 1.

```
Input : Array A of integers of length n
  Output: Array containing sorted elements of A
1 for k = 2 to n do
     for j = k to 2 do
2
         if A[j] < A[j-1] then
3
            Swap A[j] and A[j-1];
4
         else
5
            Break;
6
         end
7
     end
8
9 end
10 return A;
        Algorithm 1: InsertionSort(A)
```

I proved the following Lemma:

Lemma 3.0.1. Soy yo.

I used this lemma to prove the following theorem:

**Theorem 3.0.2.** Fix any  $\kappa > 1$  and  $\lambda > 0$ . For any family of connected graphs G and  $X \subseteq \{0,1\}^{E(G)}$  such that  $\forall x \in X$ , either  $\lambda_2(G(x)) \ge \lambda$ , or G(x) has at least  $\kappa$  components,  $\text{CONN}_{G,X}$  can be solved in bounded error in time  $\widetilde{O}\left(\sqrt{\frac{nd_{avg}(G)}{\kappa\lambda_2(G)}}\left(\mathsf{S}+\sqrt{\frac{d_{max}(G)}{\lambda}}\mathsf{U}\right)\right)$ .

I discuss the idea of the proof here. The full proof can be found in Appendix A.

## YOUR WORK PART 2

## CONCLUSION

In this thesis, I have addressed the question ...

# 5.1 Open Problems

There are many areas in which one could continue this work...

#### APPENDIX A

#### DETAILS OF CODE, PROOFS, ETC.

You might have some code:

function swap=swapmat(n,q1,q2)

// Creates a matrix that swaps qubits

// q1 and q2 of an n qubit system

// The new swap matrix will be stored in swap
swap=eye(2^n);

```
for i = 1:2<sup>n</sup>
```

index=i;

if indexswap>index

```
swap(indexswap,:) = test(index,:);
```

```
swap(index ,:) = test(indexswap ,:);
```

end

#### end

#### end

We now prove Theorem 3.0.2, restated here for convenience:

**Theorem 3.0.2.** Fix any  $\kappa > 1$  and  $\lambda > 0$ . For any family of connected graphs *G* and  $X \subseteq \{0,1\}^{E(G)}$  such that  $\forall x \in X$ , either  $\lambda_2(G(x)) \ge \lambda$ , or G(x) has at least  $\kappa$  components,  $\text{CONN}_{G,X}$  can be solved in bounded error in time  $\widetilde{O}\left(\sqrt{\frac{nd_{avg}(G)}{\kappa\lambda_2(G)}}\left(\mathsf{S}+\sqrt{\frac{d_{max}(G)}{\lambda}}\mathsf{U}\right)\right)$ . *Proof.* The complexity of generating *g* is lnit =  $O(\mathsf{S}+\mathsf{U}+\log n)$ , and the initial

state has overlap at least  $\varepsilon = \Omega\left(\frac{\kappa\lambda_2(G)}{nd_{avg}}\right)$  with any unit vector in ker  $A(x) \cap$  row(A). Plugging these values into the expression in Eq. 6 gives (neglecting

polylogarithmic factors)

$$O\left(\frac{1}{\sqrt{\varepsilon}}\left(\mathsf{Init} + \sqrt{\frac{d_{\max}(G)}{\lambda}}\mathsf{U}\right)\right) = \widetilde{O}\left(\sqrt{\frac{nd_{\operatorname{avg}}}{\kappa\lambda_2(G)}}\left(\mathsf{S} + \sqrt{\frac{d_{\max}(G)}{\lambda}}\mathsf{U}\right)\right). \quad \Box$$

#### APPENDIX B

#### NOTES ON WRITING

## **B.1** Expectations

The thesis should

- Demonstrate your understanding in your own words. Plagiarism is unacceptable. See Appendix B.2.
- Be correct.
- Be written for your audience: professors in the department who are not experts in this area. You should keep your audience in mind when deciding how much background material to include, how much context to provide, and your use of field-specific terminology, notation, etc..
- Demonstrate high-quality scientific writing (see Appendix B.3):
  - Overall structure is coherent
  - Writing is clear
  - Minimal use of "weasel words" and other imprecise writing.
  - Minimal typos
- Cite references appropriately
- Be an appropriate length. Your thesis should be between 20 and 50 pages, excluding figures, appendices, and bibliography. (Extensions or retractions may be granted by your advisor.)

#### **B.2** Plagiarism

As much as possible, the thesis should be in your own words. Prior results must be cited. Additionally, any material taken from a source, whether verbatim or paraphrased, must include a citation. If you copy text word for word you must use quotation marks to indicate that it is not your own writing. However, it is relatively rare to use quotations in scientific writing, so please do this sparingly.

You should also determine your own structure at the paragraph level. A paraphrasing that mimics point by point the sentences in a source is not acceptable. For the expository parts of your thesis, we suggest gathering the information and then expressing the ideas in your own words.

Generative language models like ChatGPT may be used for brainstorming, but their words should not appear anywhere in your thesis.

### **B.3 Best Practices**

Good scientific writing is good writing and everything you have learned in other classes still applies. Some points of particular emphasis for scientific writing:

- You are telling a results-oriented story, not a time-oriented story. In other words, you should structure your thesis in order to maximize clarity and impact, not based on what you did first.
- Great papers have great figures. One way to write your thesis is to first create figures, and then write your story based on the figures.

Some more views on technical reading and writing you might find helpful

- Philip Fong, "How to Read a CS Research Paper" http://www2.cs.uregina.
   ca/~pwlfong/CS499/reading-paper.pdf
- Matt Might, Weasel Words (and passive voice) http://matt.might.net/ articles/shell-scripts-for-passive-voice-weasel-words-duplicates/

## **B.4** Writing FAQ

- I or We? Don't say "We implemented ..." when it was just you. Instead say "I implemented ...". It is fine to say "we" when it includes the reader: "We now examine ..."
- **Can we use the active voice, e.g. say "I did X…"?** Yes! Technical writing typically uses active voice. That said, you will encounter different views on active vs. passive voice so make sure to find out the expectations of other faculty or the conventions in your subfield.
- What tense do I use? If you look at Chapter 3 you will see the text is a combination of present and past depending on whether you are explaining something to the reader (present), or describing something you did (past). For example, you may write: "This thesis examines three questions. We first investigate..." Or: "I ran three experiments."
- I am seeing weird characters, e.g. many "?"s, in my LaTeX document. What is happening? Be careful when copying from a WYSIWYG editor, like Word, into your LATEX source. Word will replace certain punctuation, like double quotes, and combinations of letters, like "ff", into different character codes for fancy versions of those characters that LATEX can't render. Make sure you copy over plain text.

#### How do I cite a GitHub repository (and URLs more generally)? You can cite a

```
URL as a @misc BibTex entry [3], e.g.
```

```
@misc{HammerLab2017,
    author = {HammerLab},
    title = {pileup.js},
    url = {https://github.com/hammerlab/pileup.js/},
    lastchecked = {2017-02-06},
    year = {2017}
}
```

```
How do I cite a stack exchange posting? Again use a @misc Bibtex entry [1]
```

```
@MISC{KothariTCSSE,
	TITLE = {Open problems on the frontiers of {TCS}},
	AUTHOR = {Robin Kothari (https://cstheory.stackexchange.com/users/206/ro
	HOWPUBLISHED = {Theoretical Computer Science Stack Exchange},
	URL = {https://cstheory.stackexchange.com/q/1015}
}
```

#### BIBLIOGRAPHY

- [1] Robin Kothari (https://cstheory.stackexchange.com/users/206/robin-kothari).
   Open problems on the frontiers of TCS. Theoretical Computer Science Stack
   Exchange. URL: https://cstheory.stackexchange.com/q/1015.
- [2] Lewis Carroll. Alice's Adventures in Wonderland. George MacDonald, 1865.URL: http://arxiv.org/down-the-rabbit-hole.
- [3] HammerLab. pileup.js. 2017. URL: https://github.com/hammerlab/pileup. js/.